



Predicting shear capacity of rectangular hollow RC columns using neural networks

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Abstract

This study predicts the shear strength of rectangular hollow reinforced concrete (RC) columns using artificial neural network (ANN). A total of 120 experimental results are collected from literature and used for establishing the machine learning model. The results reveal that the proposed ANN model predicts the shear strength of rectangular hollow RC columns accurately with R^2 of 0.99. Additionally, the relative importance of input parameters on the calculated shear strength of RC columns is evaluated using Shapley value. Based on the ANN model, a graphical user interface tool is also developed and readily used in predicting the shear strength of rectangular hollow RC columns.

Keywords Rectangular hollow reinforced concrete column · Shear strength · Artificial neural network · Graphical user interface

Introduction

Rectangular hollow reinforced concrete (RC) columns have been widely used in bridge structures, since they satisfy both the efficiently lateral loading capacity and beneficial construction costs (Cassese et al., 2020; Kim et al., 2014a, 2014b; Mo et al., 2001; Pinto et al., 2003; Sun et al., 2019; Yang et al., 2019; Yeh et al., 2002a, 2002b). Understanding of failure modes is the crucial issue for designing new structures, retrofitting the existing ones properly. Numerous experimental studies reported that the RC column can be failed in flexure, shear, or flexure–shear, depending on geometric dimensions, reinforcing bar details, and material properties.

Several conventional approaches were employed to identify the failure modes of RC columns with solid cross-sections. Simply, failure types of rectangular RC columns can be predicted using the aspect ratio, a/d (i.e., shear span-to-effective depth ratio). If $a/d \geq 4$, the column fails in flexure; if $2 < a/d < 4$, a flexure–shear failure is governed; if $a/d \leq 2$, the shear failure is dominated (Qi et al., 2013). However, the effects of material properties and reinforcement details were not reflected in this approach (Feng et al., 2020). Another indicator, the shear strength ratio (V_r), i.e., the ratio of the shear demand to shear capacity, can be used for predicting the failure modes of rectangular RC columns (Pekelnicky et al., 2012; Qi et al., 2013). The column suffers shear failure if $V_r > 1$, the column fails in flexure if $V_r \leq 0.6$, and otherwise, a flexure–shear failure is dominated. However, it was also pointed out that this method owned a deficiency and, therefore, predicted failure modes of solid RC columns less accurately (Ma & Gong, 2018; Qi et al., 2013; Zhu et al., 2007). Furthermore, Ghee et al. (1989) used the displacement ductility factor, μ (i.e., the ratio of the displacement at the maximum shear strength to the yield displacement), to classify failure modes of circular RC columns. If $\mu \geq 6$, the column fails in flexure; a ductile–shear failure can be exhibited if $2 < \mu < 6$; and otherwise, if $\mu \leq 2$, a shear failure is governed. Nevertheless, they conducted a small set of experiments thus, it was insufficient to apply for a wide range of columns.

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Machine learning (ML) techniques have been extensively applied in various engineering problems since it owns great advantages such as computational efficiency and sufficient consideration of uncertainties (Falcone et al., 2020; Kaveh & Khavaninzadeh, 2023). Numerous studies used ML techniques to estimate the structural response of civil structures (Caglar et al., 2009; Farfani et al., 2015; Gharehbaghi et al., 2019; Morfidis & Kostinakis, 2018; Razzaghi et al., 2018). The mentioned studies highlighted the capability of used ML techniques in estimating responses and failure modes of structures, and some methods showed to be superior compared with others. Artificial neural network (ANN) is one of the most efficient ML models in predicting structural responses of RC structures (Asteris & Mokos, 2019; Kaveh et al., 2021, 2023; Mai et al., 2022; Nguyen et al., 2021a, 2021b; Tran et al., 2020, 2022).

Recently, several studies have applied ML techniques to predict the shear capacity of RC columns with solid sections, in which typical works are Mangalathu and Jeon (2019), Feng et al. (2020), Mangalathu et al. (2020), and Phan et al. (2022). They highlighted the excellent performance of ML in prediction problems. However, there are no ML studies on predicting shear strength of hollow RC columns so far.

Empirical formulas in previous studies and design codes are mostly focused on calculation of the shear strength of solid RC columns (ACI-318-14, 2014; ASCE/SEI-41-06, 2007; Ascheim & Moehle, 1992; Biskinis et al., 2004; Cassese et al., 2019; EN-, 1998-1, 2004; Kowalsky & Priestley, 2000; Priestley et al., 1994; Sezen & Moehle, 2004). Those expressions have been widely applied for hollow RC columns. However, a large scatter is still existing in comparison between experimental tests and predictive equations, even though a specific model (Shin et al., 2013) is proposed for calculating the shear strength of hollow RC columns.

This study applies ANN model, which is developed based on 120 experimental data, to predict the shear strength of rectangular RC columns with hollow cross-section types. The result of ANN is then compared with that of predicted by seven published empirical formulas. Additionally, the relative importance of input parameters on the calculated shear strength of RC columns is evaluated using Shapley value. Moreover, a graphical user interface (GUI) tool, which can be readily used in the design process and structural performance evaluation, is developed for predicting the shear strength of rectangular hollow RC columns.

Description of experimental data

To develop ML techniques, a set of 120 experimental test results of RC columns with the rectangular hollow cross-section was collected from the literature (Calvi et al., 2005;

Cheng et al., 2005; Faria et al., 2004; Han et al., 2013; Kim, 2019; Kim et al., 2019; Mo & Nien, 2002; Mo et al., 2003; Pinto et al., 2003; Shin et al., 2013; Yang et al., 2019; Yeh et al., 2002a). Eleven input parameters, including geometric dimensions, reinforcing bar details, material properties, and axial load, need to be provided to estimate the shear strength of RC columns. Geometric dimensions comprise of the height of the column (L_v), the width of the cross-section (B), the length of the cross-section (H), and the wall thickness (t_w). Reinforcement details include the longitudinal reinforcement ratio (ρ_l), the transversal reinforcing bar ratio (ρ_w), and the spacing of the transversal reinforcements (s). Material properties are the yield strength of the longitudinal (f_{y_l}) and transversal (f_{y_w}) reinforcing bars and the compressive strength of concrete (f_c'). The axial load (P) is also considered in the database.

Figure 1 schematically shows the configurations and reinforcement properties of the rectangular hollow RC column. The statistical properties of the experimental results are described in Table 1. In this table, eleven input parameters are numbered as variables from X1 to X11 to

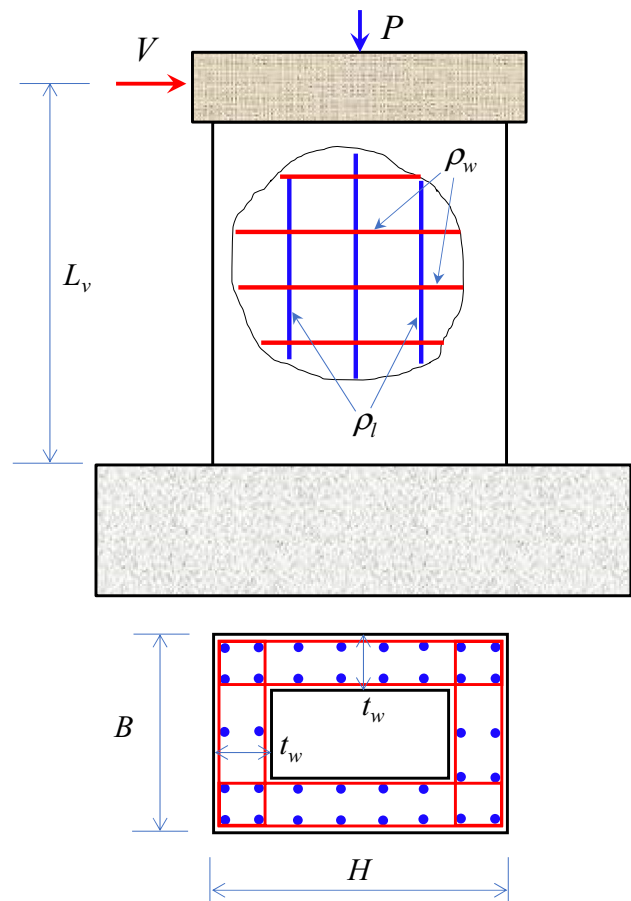


Fig. 1 Configurations and properties of rectangular hollow RC columns

Table 1 Statistical properties of input parameters of used database

| Input parameter | L_v (mm) | B (mm) | H (mm) | t_w (mm) | ρ_l (%) | ρ_w (%) | s (mm) | f_c' (MPa) | f_{yl} (MPa) | f_{yw} (MPa) | P (kN) |
|-----------------|------------|----------|----------|------------|--------------|--------------|----------|--------------|----------------|----------------|----------|
| (Variable) | (X1) | (X2) | (X3) | (X4) | (X5) | (X6) | (X7) | (X8) | (X9) | (X10) | (X11) |
| Min | 650 | 320 | 250 | 70 | 0.19 | 0.0 | 30 | 17 | 270 | 235 | 0.0 |
| Mean | 2455 | 626.7 | 725.7 | 139.7 | 1.65 | 0.18 | 191.20 | 35.7 | 411.9 | 398.4 | 1250.6 |
| Max | 13,250 | 1500 | 2740 | 300 | 6.41 | 1.60 | 1800 | 70 | 625 | 700 | 8799.8 |
| <i>SD</i> | 1740.8 | 309.6 | 426.2 | 62.7 | 0.84 | 0.22 | 354.5 | 11.9 | 97.8 | 101.7 | 1394.9 |
| <i>COV</i> | 0.71 | 0.49 | 0.59 | 0.45 | 0.51 | 1.22 | 1.85 | 0.33 | 0.24 | 0.26 | 1.12 |

consider in performing machine learning models. The frequency histograms of input parameters and failure modes of the 120 collected data are shown in Fig. 2. For this database, the number of columns failed in flexure (F), flexure–shear combination (FS), and shear (S) is 60, 42, and 18, respectively.

Overview of ANN model

In addition to aforesaid classification techniques, the ANN model was used for predicting the shear strength of rectangular hollow RC columns. An ANN model comprises

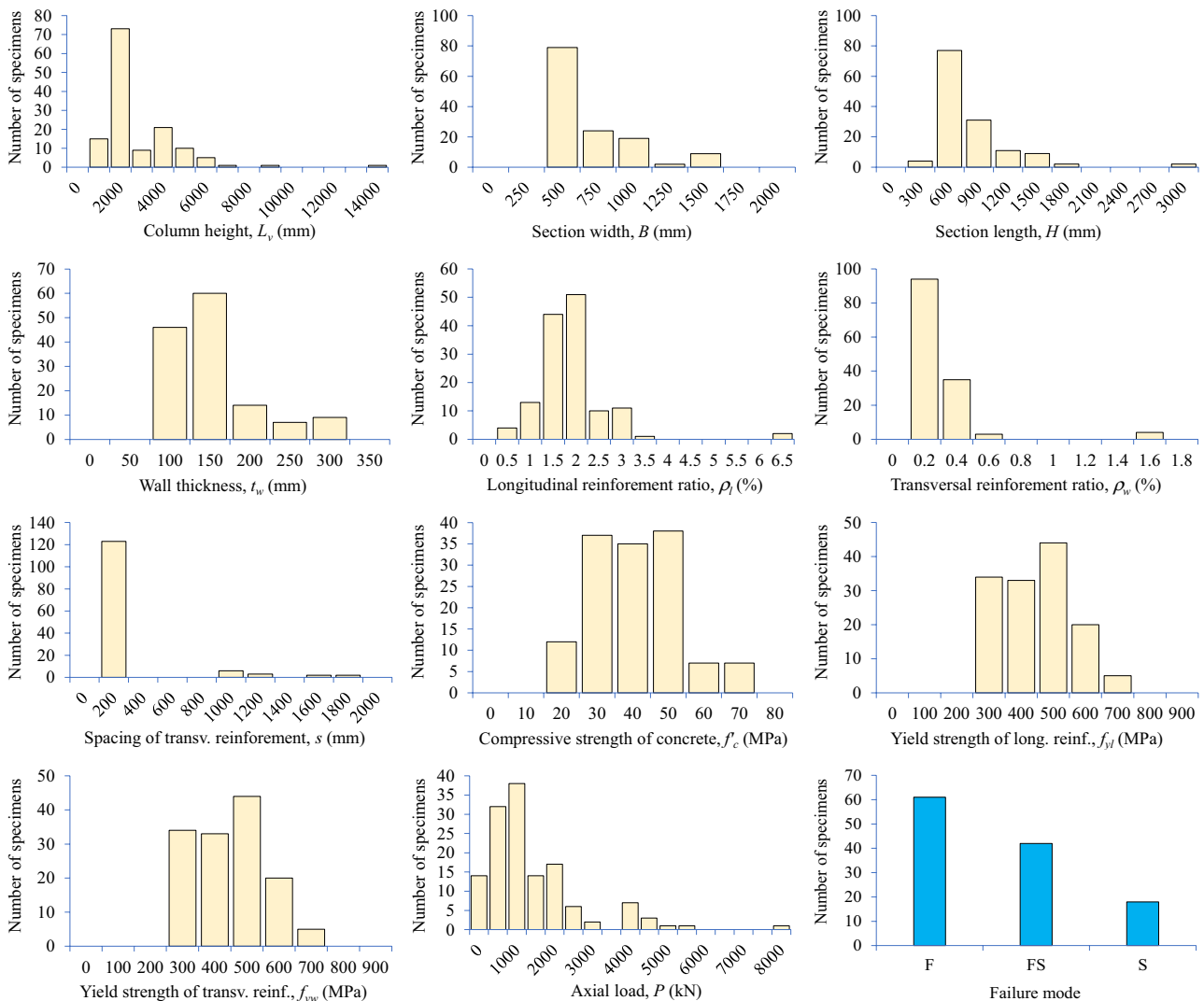


Fig. 2 Histograms of input parameters and observed failure modes of experimental data

of three components:

- (1) Input layer, where input parameters are entered,
- (2) Hidden layer(s), and
- (3) Output layer, where the predicted result is obtained.

In this study, the tansig and purelin functions were employed for hidden and output layer, respectively. These functions aim to make a transition during training the network smoothly, expressed by Eqs. (1) and (2).

$$y = \text{tansig}(x) = \frac{2}{1 + e^{-2x}} - 1 \tag{1}$$

$$y = \text{purelin}(x) = x. \tag{2}$$

To perform the ANN algorithm, following processes are required:

- (1) Firstly, the input data are provided to the input layer, the signals are transferred through the connections, from one node (i.e., neuron) to another in the network. This is called the forward pass.

- (2) Secondly, after obtaining the output from the forward pass, it is required to evaluate this output by comparing it with the target using the mean squared error (MSE), as expressed in Eq. (3). This is called the backward pass.
- (3) Moreover, it is needed to minimize the error by iteratively updating those processes until *MSE* is converged.

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N (p_i - t_i)^2, \tag{3}$$

where *N* is the number of samples; *t_i* and *p_i* are the target and predicted values of the *i*th sample, respectively. Figure 3 shows the structure of the ANN model, in which the input layer contains eleven parameters, the hidden layer includes eight neurons, and the output layer is the predicted shear strength.

Fig. 3 Depiction of ANN structure

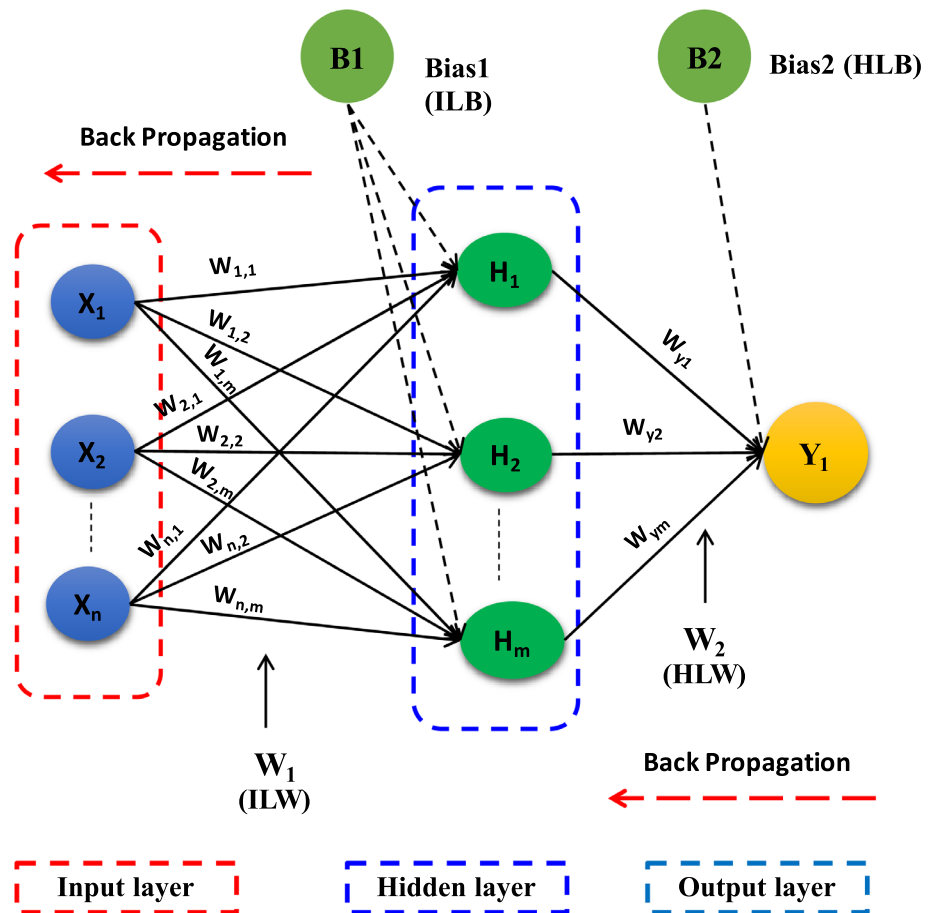


Table 2 Equations for calculating the shear strength of rectangular hollow RC columns

| No | Reference | Equation |
|----|-------------------------------|--|
| 1 | Ascheim and Moehle (1992) | $V_{R1} = V_c + V_w \quad (4)$ $V_c = 0.3 \left(k + \frac{P}{13.8A_g} \right) 0.8A_g \sqrt{f_c'} t$ $k = \frac{4-\mu}{3}, \mu \text{ is the displacement ductility}$ $V_w = \frac{A_{sw} f_{yw} d}{s \tan(30^\circ)}; d = 0.8H$ |
| 2 | Priestley et al. (1994) | $V_{R2} = V_c + V_w + V_p \quad (5)$ $V_c = 0.8A_g k \sqrt{f_c'}$ $k = 0.29 \text{ for } \mu < 2$ $k = 0.29 - 0.12(\mu - 2) \text{ for } 2 < \mu < 4$ $k = 0.10 \text{ for } \mu > 4$ $V_w = \frac{A_{sw} f_{yw} D t}{s} \cot(30^\circ)$ $V_p = P \tan(\alpha) = \frac{D-c}{2a} P$ |
| 3 | Kowalsky and Priestley (2000) | $V_{R3} = V_c + V_w \quad (6)$ $V_c = \alpha \beta k 0.8A_g \sqrt{f_c'}$ $1 \leq \alpha = 3 - \frac{L_v}{H} \leq 1.5;$ $\beta = 0.5 + 20\rho_l \leq 1$ $k = 0.29 \text{ for } \mu < 2.0$ $k = 0.05 \text{ for } \mu > 8.0$ $V_w = \frac{A_{sw} f_{yw} (D-t-c)}{s} \cot(30^\circ)$ |
| 4 | Sezen and Moehle (2004) | $V_{R4} = V_c + V_s \quad (7)$ $V_c = k \left(\frac{0.5\sqrt{f_c'} t}{a/d} \sqrt{1 + \frac{P}{0.5A_g \sqrt{f_c'}}} \right) 0.8A_g; d = D - \text{cover}$ $V_s = k \frac{A_{sw} f_{yw} d}{s}$ $k = 1 \text{ for } \mu < 2.0$ $k = 0.7 \text{ for } \mu > 6.0$ <p><i>a</i> is the shear span, i.e., the distance from loading point to the boundary</p> |
| 5 | Biskinis et al. (2004) | $V_{R5} = V_p + k(V_c + V_w) \quad (8)$ $V_c = 0.16 \max(0.5; 100\rho_l) \left(1 - 0.16 \min\left(5; \frac{a}{d}\right) \right) A_c \sqrt{f_c'}$ $V_w = \frac{A_{sw}}{s} (d - d') f_{yw}$ $V_p = \frac{D-x}{2a} \min(P; 0.55A_c f_c')$ <p><i>x</i> is the neutral axis depth, <i>d'</i> is the depth of the compression reinforcement layer</p> $k = 1 \sim 0.75 \text{ for } \mu < 1 \sim 6$ $A_c = b_w d, (d = 0.8H \text{ is the effective depth});$ |
| 6 | Shin et al. (2013) | $V_{R6} = (\alpha \beta k) 5 \sqrt{f_c'} \sqrt{1 + \frac{P}{0.5A_g \sqrt{f_c'}}} (A_e) + \frac{A_s f_{yv} d}{s}; d = 0.8H; \quad (9)$ $\alpha = 1.35 - 0.3 \frac{L_v}{H} (1.5 \leq \frac{L_v}{H} \leq 3);$ $\beta = 0.5 + 20\rho_l \leq 1;$ $\gamma = \frac{8-\mu}{6} (2 \leq \mu \leq 5);$ |
| 7 | Cassese et al. (2019) | $V_{R7} = \alpha \beta k \sqrt{f_c'} (2t_w d); d = 0.8H; \quad (10)$ $1 \leq \alpha = 3 - \frac{L_v}{H} \leq 1.5;$ $\beta = 0.5 + 20\rho_l \leq 1; \rho_l = \frac{A}{BH}$ |

Results and discussion

Previous studies mostly proposed equations for calculating the shear strength of solid RC columns (ACI-318-14, 2014; ASCE/SEI-41-06, 2007; Ascheim & Moehle, 1992; Biskinis et al., 2004; Cassese et al., 2019; EN-, 1998–1,

2004; Kowalsky & Priestley, 2000; Priestley et al., 1994; Sezen & Moehle, 2004). Those equations also have been applied for hollow RC columns. However, the hollow columns may expose a different behavior from the solid ones subjected to lateral loads (Cassese, 2017; Shin et al., 2013). So far, only one specific equation for predicting

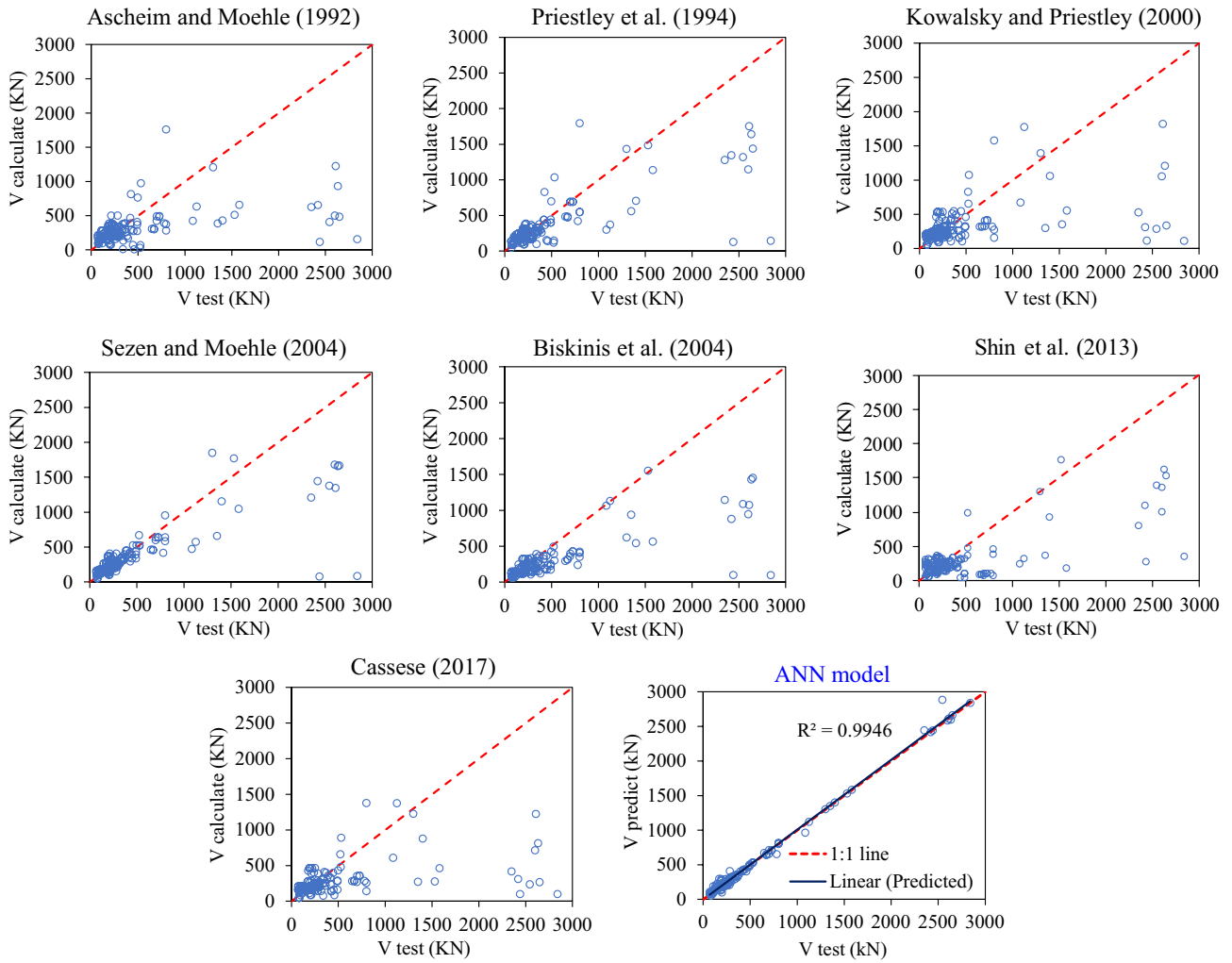
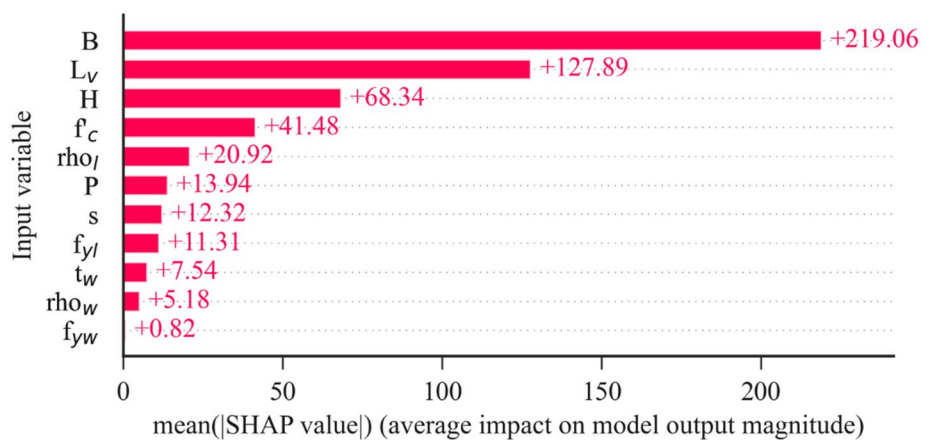


Fig. 4 Comparison of shear strength between experiments and various calculated models

Fig. 5 Relative importance of each feature



shear strength of hollow RC columns was developed by Shin et al. (Shin et al., 2013). In this study, we employed seven typical equations for estimating the shear strength of the hollow RC columns, as expressed in Table 2.

The comparisons of predictive models and experimental results are presented in Fig. 4. It was obviously demonstrated that the result of the ANN model has a smallest scattering with R^2 of 0.995, while existing models contain a wider deviation from the 1:1 line. This observation highlighted that the ANN model can be the optimal model for calculating the shear strength of rectangular hollow RC columns. The second best option was the model of Sezen and Moehle (2004), even though some discrepancies between calculated and experimental results were existing.

To explore how the predictions of the shear strength are affected by the input variables in the ANN model, the SHAP method is also adopted. The importance of the input variables in predicting the shear strength of hollow RC columns is presented in Fig. 5. These figures show that the most influential feature to the shear strength is B , followed by the L_v , H , f_c' , ρ_l , P , s , f_{yl} , t_w , ρ_w , and f_{yw} . It is also observed that ρ_l , P , s , f_{yl} , t_w , ρ_w , and f_{yw} slightly impact the ANN model's outputs.

To apply proposed ML models in specific problems, a convenient tool needs to be established. We developed a Graphical User Interface (GUI) in MATLAB for facilitating failure modes identification as well as prediction of the shear strength of rectangular hollow RC columns, as shown in Fig. 6. Eleven input parameters need to be provided. The failure modes and the shear strength of the column are

readily obtained after filling the required inputs. It takes a few seconds to achieve the predictive results. It should be noted that the GUI tool is provided freely at https://github.com/duyduan1304/GUI_RCHollowColumn.

Conclusions

The failure modes of rectangular hollow RC columns were identified using six novel machine learning (ML) techniques, which were established based on 120 experimental results. Six ML models included Naïve Bayes (NB), K-nearest Neighbors (KNN), Decision Tree (DT), and Support Vector Machine (SVM) with Linear, Gaussian, and Polynomial kernel functions. Meanwhile, the Artificial Neural Network (ANN) technique was employed to predict the shear strength of the columns. Significant conclusions are reached as follows.

- The ANN technique predicted the shear strength of rectangular hollow RC columns more accurately than that of existing formulas with R^2 value larger than 0.99.
- The width and height of cross-section (i.e., B and H) and the column height (L_v) were the most influential parameters on the calculated shear strength of the hollow columns.
- An effective GUI tool was developed and readily applied for predicting the shear strength and identifying failure modes of rectangular hollow RC columns in the design process and structural performance evaluation (https://github.com/duyduan1304/GUI_RCHollowColumn).

Fig. 6 GUI tool for predicting the strength of rectangular hollow RC columns

Detailed information of the database

| ID | L_v (mm) | B (mm) | H (mm) | t_w (mm) | ρ_l (%) | ρ_w (%) | s (mm) | f'_c (MPa) | f_{yt} (MPa) | f_{yw} (MPa) | P (kN) | V (kN) | FM |
|----|------------|----------|----------|------------|--------------|--------------|----------|--------------|----------------|----------------|----------|-------------|------|
| 1 | 1500 | 400 | 600 | 100 | 0.88 | 0.12 | 120 | 19 | 540 | 655 | 148 | 168 | F |
| 2 | 1500 | 600 | 400 | 100 | 0.88 | 0.12 | 120 | 21 | 540 | 655 | 166 | 117 | F |
| 3 | 900 | 400 | 600 | 100 | 0.88 | 0.12 | 120 | 22 | 540 | 655 | 174 | 278 | FS |
| 4 | 900 | 600 | 400 | 100 | 0.88 | 0.12 | 120 | 21 | 540 | 655 | 168 | 193 | FS |
| 5 | 900 | 450 | 450 | 75 | 1.07 | 0.13 | 75 | 35 | 550 | 550 | 236 | 217 | FS |
| 6 | 900 | 450 | 450 | 75 | 1.07 | 0.13 | 75 | 24 | 550 | 550 | 507 | 247 | FS |
| 7 | 900 | 450 | 450 | 75 | 1.07 | 0.13 | 75 | 32 | 550 | 550 | 763 | 297 | FS |
| 8 | 1350 | 450 | 450 | 75 | 1.79 | 0.25 | 75 | 30 | 550 | 550 | 239 | 217 | FS |
| 9 | 1350 | 450 | 450 | 75 | 1.79 | 0.25 | 75 | 30 | 550 | 550 | 501 | 209 | FS |
| 10 | 1350 | 450 | 450 | 75 | 1.79 | 0.25 | 75 | 33 | 550 | 550 | 515 | 226 | FS |
| 11 | 1350 | 450 | 450 | 75 | 1.79 | 0.25 | 75 | 31 | 550 | 550 | 762 | 258 | FS |
| 12 | 1400 | 450 | 450 | 75 | 1.79 | 0.20 | 75 | 20 | 625 | 390 | 245 | 190 | FS |
| 13 | 1400 | 450 | 450 | 75 | 1.79 | 0.09 | 75 | 28 | 435 | 437 | 251 | 130 | FS |
| 14 | 1400 | 450 | 450 | 75 | 1.79 | 0.09 | 75 | 29 | 560 | 443 | 257 | 170 | S |
| 15 | 1400 | 450 | 450 | 75 | 1.79 | 0.19 | 75 | 29 | 560 | 443 | 257 | 210 | S |
| 16 | 1400 | 450 | 900 | 75 | 1.79 | 0.20 | 75 | 20 | 625 | 390 | 249 | 240 | S |
| 17 | 1400 | 450 | 900 | 75 | 1.79 | 0.09 | 75 | 28 | 435 | 437 | 251 | 190 | S |
| 18 | 1400 | 450 | 900 | 75 | 1.79 | 0.09 | 75 | 29 | 560 | 443 | 257 | 190 | S |
| 19 | 1400 | 450 | 900 | 75 | 1.79 | 0.19 | 75 | 29 | 560 | 443 | 257 | 250 | S |
| 20 | 900 | 600 | 400 | 100 | 0.88 | 0.12 | 120 | 17 | 540 | 655 | 136 | 278 | FS |
| 21 | 900 | 400 | 600 | 100 | 0.88 | 0.12 | 120 | 17 | 540 | 655 | 136 | 193 | FS |
| 22 | 1800 | 500 | 500 | 120 | 0.19 | 0.11 | 50 | 58 | 476 | 480 | 975 | 333 | F |
| 23 | 1800 | 500 | 500 | 120 | 0.19 | 0.11 | 50 | 63 | 476 | 480 | 1471 | 360 | F |
| 24 | 1800 | 500 | 500 | 120 | 0.19 | 0.06 | 40 | 70 | 476 | 480 | 983 | 332 | F |
| 25 | 1800 | 500 | 500 | 120 | 1.88 | 0.52 | 40 | 61 | 476 | 363 | 1449 | 350 | FS |
| 26 | 1500 | 500 | 500 | 120 | 1.88 | 0.52 | 40 | 51 | 476 | 363 | 1013 | 364 | S |
| 27 | 1500 | 500 | 500 | 120 | 1.88 | 0.52 | 40 | 50 | 476 | 363 | 544 | 302 | FS |
| 28 | 5400 | 1500 | 1500 | 300 | 1.90 | 0.28 | 150 | 34 | 476 | 480 | 4355 | 2350 | FS |
| 29 | 5400 | 1500 | 1500 | 300 | 1.90 | 0.28 | 150 | 29 | 476 | 480 | 8800 | 2610 | S |
| 30 | 5400 | 500 | 500 | 120 | 1.90 | 0.03 | 150 | 33 | 476 | 480 | 553 | 2440 | F |
| 31 | 5400 | 500 | 500 | 120 | 1.90 | 0.03 | 150 | 31 | 476 | 480 | 982 | 2840 | F |
| 32 | 1800 | 500 | 500 | 120 | 1.90 | 0.11 | 50 | 33 | 476 | 480 | 499 | 271 | F |
| 33 | 1500 | 500 | 500 | 120 | 1.90 | 0.03 | 50 | 20 | 476 | 405 | 501 | 270 | S |
| 34 | 1500 | 500 | 500 | 120 | 1.90 | 0.03 | 50 | 27 | 423 | 405 | 500 | 298 | F |
| 35 | 1500 | 500 | 500 | 120 | 1.90 | 0.03 | 50 | 29 | 423 | 405 | 499 | 295 | F |
| 36 | 1500 | 500 | 500 | 120 | 1.90 | 0.03 | 50 | 27 | 406 | 405 | 498 | 278 | F |
| 37 | 1800 | 500 | 500 | 120 | 1.90 | 0.11 | 50 | 28 | 406 | 480 | 500 | 241 | F |
| 38 | 2000 | 550 | 550 | 140 | 1.33 | 0.09 | 100 | 48 | 617 | 405 | 4418 | 429 | F |
| 39 | 2000 | 550 | 550 | 140 | 1.33 | 0.09 | 100 | 57 | 617 | 405 | 2617 | 316 | F |
| 40 | 2000 | 550 | 550 | 110 | 1.58 | 0.09 | 100 | 60 | 617 | 405 | 5432 | 423 | FS |
| 41 | 6500 | 1500 | 1500 | 300 | 1.08 | 0.11 | 80 | 34 | 460 | 343 | 4015 | 1580 | F |
| 42 | 4500 | 1500 | 1500 | 300 | 1.08 | 0.04 | 120 | 34 | 460 | 510 | 4015 | 2420 | F |
| 43 | 3500 | 1500 | 1500 | 300 | 1.72 | 0.03 | 200 | 32 | 418 | 420 | 3686 | 2650 | S |
| 44 | 4500 | 1000 | 1000 | 250 | 1.53 | 0.17 | 80 | 22 | 376 | 343 | 1650 | 671 | F |
| 45 | 4500 | 1000 | 1000 | 250 | 1.53 | 0.17 | 80 | 47 | 408 | 406 | 2468 | 727 | F |
| 46 | 900 | 600 | 900 | 130 | 1.80 | 0.01 | 900 | 25 | 340 | 340 | 0 | 525 | FS |
| 47 | 1200 | 600 | 900 | 130 | 1.80 | 0.01 | 1200 | 25 | 340 | 340 | 0 | 445 | FS |

| ID | L_v (mm) | B (mm) | H (mm) | t_w (mm) | ρ_l (%) | ρ_w (%) | s (mm) | f'_c (MPa) | f_{yt} (MPa) | f_{yw} (MPa) | P (kN) | V (kN) | FM |
|----|------------|----------|----------|------------|--------------|--------------|----------|--------------|----------------|----------------|----------|-------------|------|
| 48 | 1500 | 600 | 900 | 130 | 1.80 | 0.01 | 1500 | 25 | 340 | 340 | 0 | 341 | FS |
| 49 | 1800 | 600 | 900 | 130 | 1.80 | 0.00 | 1800 | 25 | 340 | 340 | 0 | 259 | FS |
| 50 | 900 | 600 | 900 | 80 | 2.70 | 0.01 | 900 | 25 | 340 | 340 | 0 | 337 | S |
| 51 | 900 | 600 | 900 | 180 | 1.80 | 0.01 | 900 | 25 | 340 | 340 | 0 | 522 | FS |
| 52 | 900 | 600 | 900 | 160 | 1.07 | 0.01 | 900 | 18 | 300 | 300 | 0 | 458 | FS |
| 53 | 900 | 600 | 900 | 130 | 1.26 | 0.01 | 900 | 18 | 300 | 300 | 0 | 392 | FS |
| 54 | 1200 | 600 | 900 | 130 | 1.26 | 0.01 | 1200 | 18 | 300 | 300 | 0 | 334 | FS |
| 55 | 1500 | 600 | 900 | 130 | 1.26 | 0.01 | 1500 | 18 | 300 | 300 | 0 | 269 | FS |
| 56 | 1800 | 600 | 900 | 130 | 1.26 | 0.00 | 1800 | 18 | 300 | 300 | 0 | 203 | FS |
| 57 | 900 | 600 | 900 | 130 | 0.63 | 0.01 | 900 | 18 | 300 | 300 | 0 | 381 | FS |
| 58 | 3500 | 1500 | 1500 | 300 | 1.69 | 0.03 | 200 | 32 | 418 | 420 | 3594 | 2633 | S |
| 59 | 3500 | 1500 | 1500 | 300 | 1.69 | 0.03 | 200 | 18 | 420 | 413 | 3888 | 2544 | F |
| 60 | 3500 | 1500 | 1500 | 300 | 1.69 | 0.03 | 200 | 38 | 418 | 420 | 3621 | 1530 | S |
| 61 | 2000 | 500 | 500 | 200 | 1.13 | 0.25 | 40 | 30 | 460 | 400 | 1350 | 178 | S |
| 62 | 2000 | 500 | 500 | 200 | 1.13 | 0.25 | 40 | 30 | 460 | 400 | 675 | 171 | F |
| 63 | 2000 | 500 | 500 | 200 | 1.13 | 0.13 | 80 | 25 | 460 | 400 | 675 | 173 | F |
| 64 | 2000 | 500 | 500 | 200 | 1.13 | 0.25 | 40 | 50 | 460 | 400 | 1350 | 215 | F |
| 65 | 2000 | 500 | 500 | 200 | 1.13 | 0.25 | 40 | 50 | 460 | 400 | 675 | 177 | F |
| 66 | 2000 | 500 | 500 | 200 | 1.13 | 0.13 | 80 | 36 | 460 | 400 | 675 | 173 | F |
| 67 | 1440 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 1001 | 147 | F |
| 68 | 1440 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 1001 | 146 | F |
| 69 | 1440 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 2002 | 223 | F |
| 70 | 1440 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 2002 | 225 | F |
| 71 | 1440 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 615 | 207 | FS |
| 72 | 1440 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 615 | 261 | FS |
| 73 | 2880 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 615 | 70 | F |
| 74 | 2880 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 615 | 72 | F |
| 75 | 2880 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 1229 | 106 | F |
| 76 | 2880 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 1229 | 197 | F |
| 77 | 2880 | 360 | 500 | 120 | 2.10 | 0.25 | 55 | 41 | 300 | 300 | 615 | 69 | F |
| 78 | 3600 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 615 | 93 | F |
| 79 | 3600 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 615 | 95 | F |
| 80 | 3600 | 360 | 500 | 120 | 1.40 | 0.35 | 40 | 41 | 300 | 300 | 1229 | 110 | F |
| 81 | 3600 | 360 | 500 | 120 | 2.10 | 0.35 | 40 | 41 | 300 | 300 | 1229 | 123 | F |
| 82 | 3600 | 360 | 500 | 120 | 2.10 | 0.25 | 55 | 41 | 300 | 300 | 615 | 93 | F |
| 83 | 3025 | 750 | 750 | 120 | 2.84 | 0.06 | 60 | 31 | 335 | 320 | 937 | 282 | F |
| 84 | 3025 | 750 | 750 | 120 | 2.84 | 0.13 | 30 | 31 | 335 | 320 | 4687 | 496 | FS |
| 85 | 3025 | 750 | 750 | 120 | 2.84 | 0.09 | 40 | 28 | 335 | 320 | 2540 | 415 | FS |
| 86 | 3025 | 750 | 750 | 120 | 2.84 | 0.06 | 60 | 28 | 335 | 320 | 2540 | 418 | FS |
| 87 | 5750 | 1020 | 2740 | 170 | 0.40 | 0.09 | 120 | 35 | 500 | 500 | 3663 | 1300 | F |
| 88 | 13,250 | 1020 | 2740 | 170 | 0.70 | 0.09 | 120 | 35 | 500 | 500 | 3663 | 800 | F |
| 89 | 4200 | 730 | 975 | 150 | 6.41 | 0.27 | 40 | 57 | 393 | 390 | 1880 | 1124 | F |
| 90 | 4200 | 730 | 975 | 150 | 6.41 | 0.27 | 40 | 49 | 393 | 390 | 430 | 1084 | F |
| 91 | 1420 | 500 | 360 | 100 | 1.40 | 0.04 | 150 | 39 | 335 | 235 | 510 | 105 | F |
| 92 | 4500 | 1000 | 1000 | 250 | 1.53 | 0.17 | 80 | 47 | 408 | 406 | 2468 | 727 | F |
| 93 | 4500 | 1000 | 1000 | 250 | 1.38 | 0.17 | 80 | 47 | 408 | 406 | 2468 | 699 | F |
| 94 | 4500 | 1000 | 1000 | 250 | 1.38 | 0.11 | 120 | 47 | 408 | 406 | 2468 | 697 | F |
| 95 | 1200 | 320 | 320 | 85 | 1.57 | 0.34 | 50 | 34 | 295 | 345 | 0 | 70 | S |
| 96 | 1200 | 320 | 320 | 85 | 1.57 | 0.17 | 50 | 34 | 295 | 345 | 299 | 90 | F |
| 97 | 1200 | 320 | 320 | 85 | 1.57 | 0.34 | 50 | 34 | 295 | 345 | 299 | 85 | F |

| ID | L_v (mm) | B (mm) | H (mm) | t_w (mm) | ρ_l (%) | ρ_w (%) | s (mm) | f'_c (MPa) | f_{yt} (MPa) | f_{yw} (MPa) | P (kN) | V (kN) | FM |
|-----|------------|----------|----------|------------|--------------|--------------|----------|--------------|----------------|----------------|----------|-------------|------|
| 98 | 650 | 320 | 320 | 85 | 1.57 | 0.17 | 50 | 34 | 295 | 345 | 299 | 175 | S |
| 99 | 650 | 320 | 320 | 85 | 1.57 | 0.34 | 50 | 34 | 295 | 345 | 299 | 190 | S |
| 100 | 4000 | 890 | 1000 | 70 | 0.98 | 0.26 | 50 | 39 | 437 | 374 | 1921 | 212 | FS |
| 101 | 4500 | 1000 | 1000 | 250 | 1.53 | 0.17 | 80 | 23 | 376 | 343 | 1710 | 671 | FS |
| 102 | 4500 | 1000 | 1000 | 250 | 1.38 | 0.17 | 80 | 23 | 376 | 343 | 1710 | 647 | FS |
| 103 | 1800 | 400 | 250 | 80 | 2.65 | 0.06 | 110 | 45 | 270 | 335 | 527 | 77 | F |
| 104 | 1800 | 400 | 250 | 80 | 2.65 | 0.06 | 110 | 45 | 270 | 335 | 702 | 82 | F |
| 105 | 1800 | 400 | 250 | 80 | 2.65 | 0.06 | 110 | 45 | 270 | 335 | 1054 | 84 | F |
| 106 | 1800 | 400 | 250 | 80 | 2.65 | 0.06 | 110 | 38 | 270 | 335 | 601 | 82 | F |
| 107 | 1350 | 400 | 400 | 100 | 2.53 | 0.07 | 100 | 24 | 374 | 363 | 230 | 200 | FS |
| 108 | 3780 | 840 | 840 | 150 | 1.15 | 0.16 | 60 | 59 | 390 | 343 | 1650 | 490 | F |
| 109 | 3780 | 840 | 840 | 150 | 1.15 | 0.08 | 120 | 40 | 390 | 343 | 1650 | 490 | F |
| 110 | 2100 | 840 | 840 | 150 | 1.15 | 0.16 | 60 | 45 | 390 | 343 | 1633 | 800 | FS |
| 111 | 2100 | 840 | 840 | 150 | 1.15 | 0.08 | 120 | 45 | 390 | 343 | 1633 | 800 | FS |
| 112 | 3780 | 840 | 840 | 150 | 1.15 | 0.16 | 60 | 40 | 390 | 343 | 1650 | 490 | F |
| 113 | 3780 | 840 | 840 | 150 | 1.15 | 0.16 | 60 | 50 | 357 | 343 | 1650 | 780 | FS |
| 114 | 2100 | 840 | 840 | 150 | 3.07 | 0.16 | 60 | 50 | 357 | 343 | 1633 | 1350 | FS |
| 115 | 1240 | 500 | 360 | 100 | 0.91 | 1.60 | 60 | 64 | 335 | 235 | 840 | 96 | F |
| 116 | 1240 | 500 | 360 | 100 | 1.33 | 1.60 | 60 | 64 | 335 | 235 | 840 | 186 | F |
| 117 | 1440 | 500 | 360 | 120 | 1.40 | 0.14 | 40 | 41 | 393 | 389 | 615 | 195 | F |
| 118 | 1440 | 500 | 360 | 120 | 1.40 | 0.14 | 40 | 41 | 393 | 389 | 1229 | 294 | F |
| 119 | 3500 | 1500 | 1500 | 300 | 1.08 | 0.03 | 200 | 33 | 423 | 392 | 3756 | 2600 | S |
| 120 | 8400 | 800 | 1600 | 160 | 1.15 | 0.03 | 200 | 51 | 500 | 700 | 1700 | 530 | F |

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Data availability https://github.com/duyduan1304/GUI_RCHollowColumn.

Declarations

Conflicts of interest The authors declare that they have no conflicts of interest.

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